

# The Macroeconomics of Central Bank Issued Digital Currencies

John Barrdear, Bank of England

Michael Kumhof, Bank of England

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## Disclaimer

The views expressed herein are those of the authors, and should not be attributed to the Bank of England.

# 1 Introduction

- The emergence of Bitcoin and associated technologies was a watershed moment in the history of 'e-monies'.
- It may, for the first time, be technically feasible for central banks to offer universal access to their balance sheet.
  - Existing centralized RTGS systems: Not robust for universal access.
  - New decentralized systems: Can potentially solve this problem.
- Question: Is universal access economically desirable?

## 2 What is a Digital Currency?

- Traditional Electronic Payment Systems - **Tiered** Ledgers:
  - Payment verification by specific third parties.
  - Hierarchical network.
- Digital Currencies - **Distributed** Ledgers:
  - Payment verification by multiple third parties.
  - Peer-to-peer network.

### **3 What is a Central-Bank Digital Currency (CBDC)?**

- **Access to the central bank's balance sheet.**
- **Universal:** Banks, firms and households.
- **Electronic.**
- **National-currency denominated.**
- **Issued against government bonds (or through spending).**
- **Interest-bearing:**
  - To equate demand and supply at 1:1 exchange rate.
  - Second tool of countercyclical monetary policy.
- **Coexisting with the present banking system.**

# 4 The Model

## 4.1 Overview

- Based on Benes and Kumhof (2012) and Jakab and Kumhof (2015, 2020).
- The non-monetary model elements are standard.
- Households:
  - Deposits: Created by banks.
  - CBDC: Created by central bank.
  - Deposits and CBDC jointly serve as medium of exchange.
- Government:
  - Fiscal policy.
  - Traditional monetary policy.
  - CBDC monetary policy.

## 4.2 Banks Overview

- Loans: Bernanke, Gertler and Gilchrist (1999)
  - Difference 1: Pre-committed lending rates  $\Rightarrow$  possible losses.
  - Difference 2: Minimum capital adequacy rules (MCAR).
  - Positive net worth: (a) Because of MCAR. (b) As shock absorber.
  - Four different loan types (calibrated to US data).
- Deposits: Schmitt-Grohé and Uribe (2004)
  - Transactions cost technology.
  - Difference: “Money” = bank deposits + CBDC.
  - Four different deposit types (calibrated to US data).

## 4.3 Wholesale Banks

- **Bank balance sheet:**

$$\check{\ell}_t^l(i) = \check{d}_t(i) + \check{n}_t^b(i)$$

- Loans = Deposits + Net Worth.
- Heterogeneity  $i$  reflects idiosyncratic non-credit risks.

- **Capital adequacy regulation:**

- Penalty  $\chi \check{\ell}_t^l(j)$  at  $t + 1$  if net worth  $< \Upsilon^*$  total assets.
- $\Upsilon =$  minimum Basel ratio (8%).
- In each period a fraction of banks violates this regulation and pays.



- **Bank optimization problem:** Maximize
  - Returns on loans.
  - Minus cost of deposits.
  - Minus net losses from retail lending banks.
  - Minus penalties on banks that violate Basel.

- **Bank optimality condition**, with spread  $r_{\ell,t+1}^x - r_{d,t+1}$ :

$$E_t \left\{ r_{\ell,t+1}^x - r_{d,t+1} - \text{spread} \left( \Upsilon, \chi, \zeta^x, \bar{\mathfrak{F}}_{t+1}^b \right) \right\} = 0$$

- Spread depends on the size of the MCAR,  $\Upsilon$ .
- Spread depends on the penalty coefficient for breaching MCAR,  $\chi$ .
- Spread depends on risk weights  $\zeta^x$ .
- Spread depends on the riskiness of banks,  $F^b \left( \bar{\omega}_{t+1}^b \right)$  and  $f^b \left( \bar{\omega}_{t+1}^b \right)$ .

## 4.4 Retail Lending Banks (BGG)

- **Loan Contract** ( $x \in \{c, a, y, k\}$ ):
  - Nominal loan amount  $L_t^x(i)$ .
  - Unconditional nominal lending rate  $i_{r,t}^x$ , payable if no default.
  - Willingness-to-lend coefficients  $\kappa_t^{xr} \neq 1$  and  $\kappa_t^{xr} \kappa_t^{xf} \neq 1$ .
  - Collateral:
    - \* Real stocks: Capital, land.
    - \* Real flows: Output, labor income.
    - \* Financial stocks: Bank deposits, CBDC.

- **Retail lending banks' ex-ante zero profit conditions (as in BGG):**

$$E_t \left\{ r_{\ell,t+1} \ell_t^x(j) - \left[ \left( 1 - \mathfrak{F}_t(\bar{\omega}_{t+1}^x) \right) r_{r,t+1}^x \ell_t^x(i) + (1 - \xi^x) \int_0^{\bar{\omega}_{t+1}^x} c_t^x(i) \omega^x f_t^x(\omega^x) d\omega^x \right] \right\} = 0$$

- **Incorporated into household optimization problem.**

## 4.5 Households

$$E_0 \sum_{t=0}^{\infty} \beta_c^t \left\{ S_t^c \left(1 - \frac{v}{x}\right) \log(c_t^c(i) - v c_{t-1}^c) - \psi_h \frac{h_t^c(i)^{1+\frac{1}{\eta}}}{1 + \frac{1}{\eta}} + \psi_a \log(a_t(i)) \right\}$$

- Adjustment costs:
  - **Financial assets:**
    - \* 2bp per 1pp increase in government debt-to-GDP.
    - \* Laubach (2009).
  - **Prices and wages:**
    - \* Inflation adjustment costs.
    - \* Ireland (2001).
  - **Physical investment:**
    - \* Cost on rate of change of investment.
    - \* Christiano, Eichenbaum and Evans (2005).
  - **Monetary friction:**
    - \* Transactions cost technology.
    - \* Schmitt-Grohe and Uribe (2004).

- SGU (2004) TA Cost Technology:

$$s_t^x(i) = s_t^x(v_t^x(i)) = S_t^{md} A_x v_t^x(i) + \frac{B_x}{v_t^x(i)} - 2(A_x B_x)^{\frac{1}{2}}$$

- $S_t^{md}$  = shock to demand for total liquidity = “flight to safety”.
- $v_t^x(i)$  = velocity (next page).

- Velocity:

$$v_t^x(i) = \frac{e_t^x(i)}{f_t^x(i)}$$

- $e_t^x(i)$  = sector-specific expenditure:

- Consumption.
- Investment.
- Factor payments.
- Real estate.

- $f_t^x(i)$  = sector-specific monetary transaction balances:

$$f_t^x = \left( (1 - \gamma)^{\frac{1}{\epsilon}} (Deposits_t^x)^{\frac{\epsilon-1}{\epsilon}} + \gamma^{\frac{1}{\epsilon}} (CBDC_t^x)^{\frac{\epsilon-1}{\epsilon}} \right)^{\frac{\epsilon}{\epsilon-1}}$$

- Monetary Distortion Markups = Liquidity Taxes:

$$\tau_{x,t}^{liq} = 1 + s_t^x + s_t^{x'} v_t^x$$

- Their effects are equivalent to consumption and capital income taxes.
- 
- What is the Distortion?
    - Shortage, relative to the Friedman rule, of liquidity.
    - This can never be completely eliminated because the cost of creating bank deposits can never go to zero.



- Consumption FOC:

$$\frac{S_t^c \left(1 - \frac{v}{x}\right)}{\check{c}_t^c - \frac{v}{x} \check{c}_{t-1}^c} = \check{\lambda}_t^c \left(1 + \tau_{c,t}\right) \left(1 + s_t^c + s_t^{c'} v_t^c\right)$$

- Monetary wedge  $1 + s_t^c + s_t^{c'} v_t^c$ .
- Monetary wedge equivalent to a consumption tax.
- Similar wedges for:
  - \* Investment.
  - \* Factor inputs.
  - \* Land.

- Capital FOC:

$$\check{\lambda}_t^c = \frac{\beta_c}{x} E_t \left\{ \check{\lambda}_{t+1}^c \text{ret}_{k,t+1} \left[ \left( 1 - \kappa_t^{kr} \Gamma_{k,t+1} \right) + \tilde{\lambda}_{t+1}^k \kappa_t^{kr} \left( \Gamma_{k,t+1} - \xi^k G_{k,t+1} \right) \right] \right\}$$

- Collateral wedge  $\left( 1 - \kappa_t^{kr} \Gamma_{k,t+1} \right) + \tilde{\lambda}_{t+1}^k \kappa_t^{kr} \left( \Gamma_{k,t+1} - \xi^k G_{k,t+1} \right)$ .

- Similar wedges for:

- \* Land (used as collateral).
- \* Phillips curve (output used as collateral).
- \* Hours worked (labor income used as collateral).
- \* Deposits (used as collateral).
- \* CBDC (used as collateral).

## 4.6 Financial Investors

$$E_0 \sum_{t=0}^{\infty} \beta_u^t \left\{ S_t^c \left(1 - \frac{v}{x}\right) \log(c_t^u(i) - \nu c_{t-1}^u) - \psi_h \frac{h_t^u(i)^{1+\frac{1}{\eta}}}{1 + \frac{1}{\eta}} + \psi_f \frac{\left(\frac{f_t^u(i)}{T_t}\right)^{1-\frac{1}{\vartheta}}}{1 - \frac{1}{\vartheta}} \right\}$$

- Common parameters  $v$ ,  $\eta$ ,  $\psi_h$  are identical to those of households.
- Liquidity in utility:
  - To calibrate a very high interest semi-elasticity of deposit demand.

- Key financial investor FOCs:

- Government bonds:

$$\check{\lambda}_t^u \left( 1 + \phi_b \left( b_t^{rat} - \bar{b}_{ss}^{rat} \right) \right) = \frac{\beta_u}{x} E_t \left( \check{\lambda}_{t+1}^u r_{t+1} \right)$$

- \* Small elasticity of real policy rate w.r.t. bond stock.

- \* Bond stock affected by CBDC issuance.

- Bank deposits:

$$\check{\lambda}_t^u \left( 1 + \phi_b \left( b_t^{rat} - \bar{b}_{ss}^{rat} \right) \right) - \psi_f \left( f_t^u \right)^{-\frac{1}{\vartheta}} f_t^{u' dep} = \frac{\beta_u}{x} E_t \left( \check{\lambda}_{t+1}^u r_{d,t+1} \right)$$

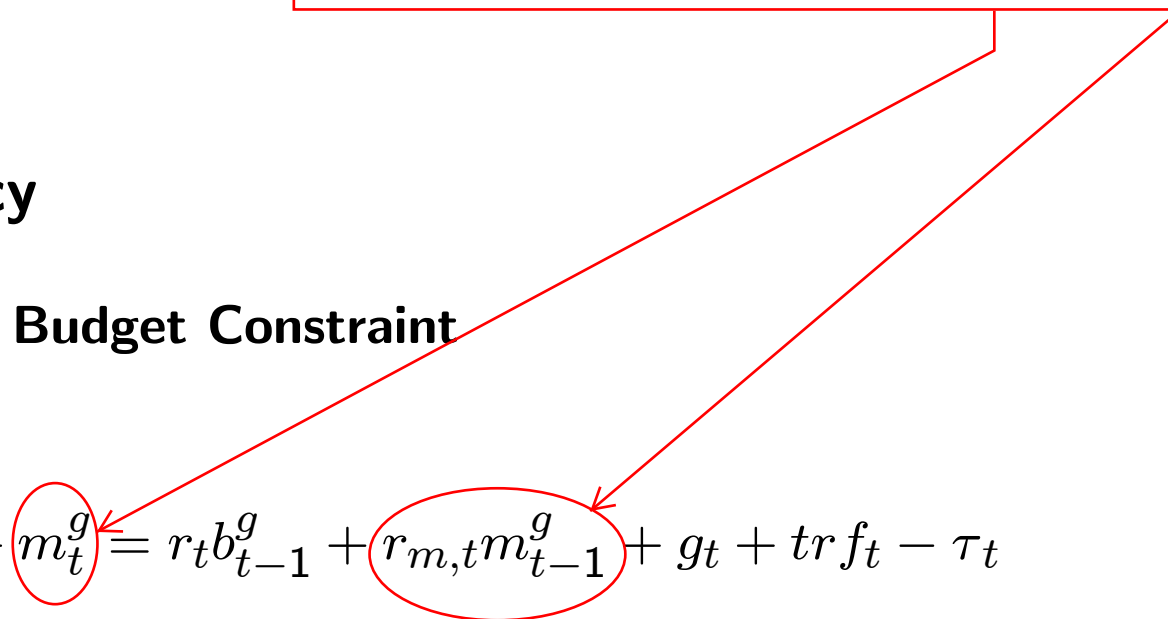
- High elasticity of deposits w.r.t. real deposit rate.

- Ensures a fairly constant spread between deposit and policy rates.

- CBDC enters like government debt.
- But it is much cheaper.

## 4.7 Fiscal Policy

### 4.7.1 Government Budget Constraint

$$b_t^g + m_t^g = r_t b_{t-1}^g + r_{m,t} m_{t-1}^g + g_t + trf_t - \tau_t$$


## 4.7.2 Fiscal Policy Rule

- Overall Deficit Ratio:

$$gdx_t^{rat} = 100 \frac{g\check{d}x_t}{g\check{d}p_t} = 100 \frac{B_t^g + M_t^g - B_{t-1}^g - M_{t-1}^g}{GDP_t}$$

- **Relevant stock change: Government Debt + CBDC.**
- Insulates budget from potentially highly volatile CBDC seigniorage flows.

- Rule for Deficit Ratio (automatic stabilizers):

$$gdx_t^{rat} = gdx_{ss}^{rat} - 100 d^{gdp} \ln \left( \frac{g\check{d}p_t}{gdp_{ss}} \right)$$

## 4.8 Monetary Policy - The Policy Rate

$$i_t = (i_{t-1})^{i_i} (i_{steady\ state})^{(1-i_i)} \left( \frac{\pi_{4,t+3}^p}{(\pi_{tgt}^p)^4} \right)^{\frac{(1-i_i)i_{\pi p}}{4}}$$

- This is a standard forward-looking Taylor rule with interest rate smoothing.

## 4.9 Monetary Policy - CBDC

- Why not target monetary aggregates? The 1980s debate versus CBDC.
- Three arguments against targeting monetary aggregates:
  1. Problems in defining the relevant aggregate: Does not apply to CBDC.
  2. Problems in controlling the aggregate: Does not apply to CBDC.
  3. Lower benefits of controlling the aggregate: Poole (1970).
    - Volatility increases if money demand shocks are important.
    - Does apply, but much more weakly than in Poole (1970).
    - Reason: Banks remain the creators of the marginal unit of money.
- To study the third argument, we need to define CBDC policy rules.



### 4.9.1 Quantity Rule for CBDC

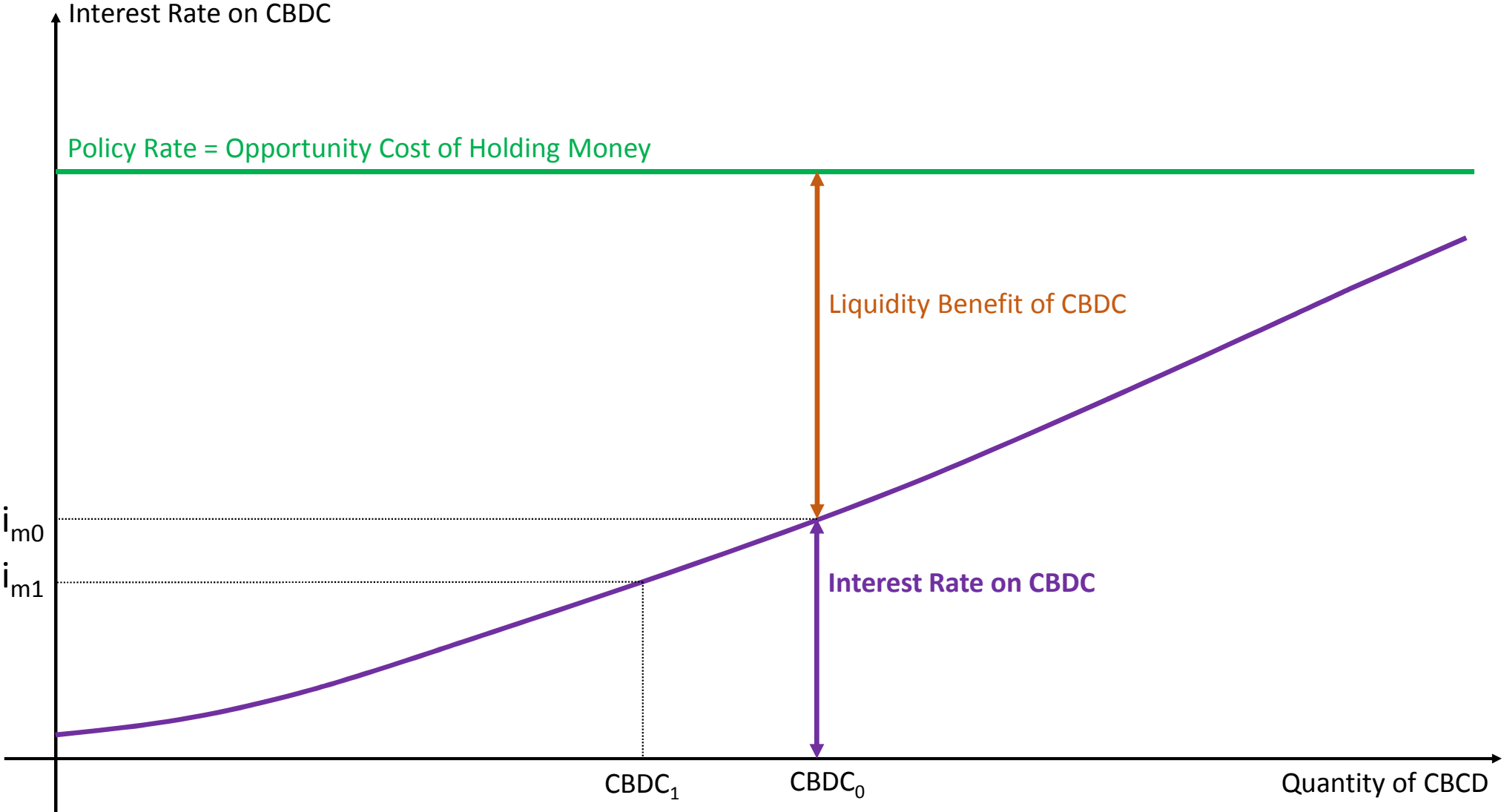
$$m_t^{rat} = m_{tgt}^{rat} S_t^{sms} - 100 m_{\pi p} E_t \ln \left( \frac{\pi_{4,t+3}^p}{(\pi_{tgt}^p)^4} \right)$$

- Fix the quantity of CBDC, let CBDC interest rate clear the market.
- $m_{\pi p} > 0$ : Removes CBDC from circulation in a boom.

### 4.9.2 Price Rule for CBDC

$$i_{m,t} = \frac{i_t}{sp} \left( \frac{\pi_{4,t+3}^p}{(\pi_{tgt}^p)^4} \right)^{-i_{\pi p}^m}$$

- Fix interest rate on CBDC, let the quantity of CBDC clear the market.
- $i_{\pi p}^m > 0$ : Makes CBDC less attractive in a boom.



## 5 Steady State Effects of the Transition to CBDC

- Assumptions:
  - Issue CBDC against government debt.
  - Magnitude: 30% of GDP.
- Results:

	<b>Steady State Output Effect</b>
1. Lower Real Policy Rates	+1.8%
2. Higher Deposit Rates Relative to Policy Rates	-0.9%
3. Reductions in Fiscal Tax Rates	+1.1%
4. Reductions in Liquidity Tax Rates	+0.9%
<b>Total</b>	<b>+2.9%</b>

# Reasons for Steady State Output Gains

## 1. Lower real interest rates:

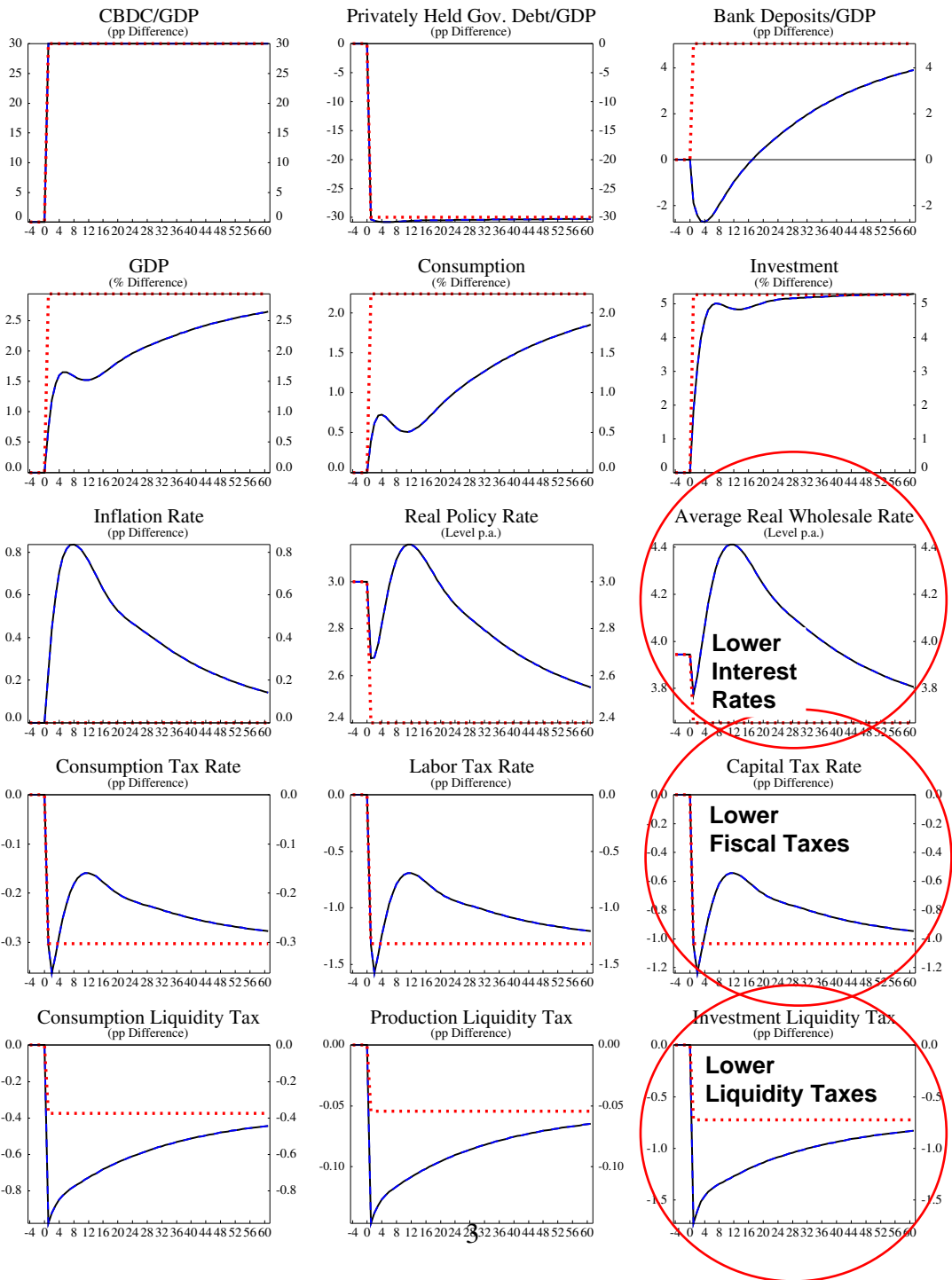
- Assumption: CBDC issued against government debt.
- CBDC is not defaultable, government debt is.
- CBDC carries a lower interest rate than government debt.

## 2. Lower fiscal tax rates:

- Much larger central bank balance sheet.
- Therefore much larger seigniorage flows.
- Assumption: Seigniorage is used to reduce distortionary taxes.

## 3. Lower liquidity tax rates:

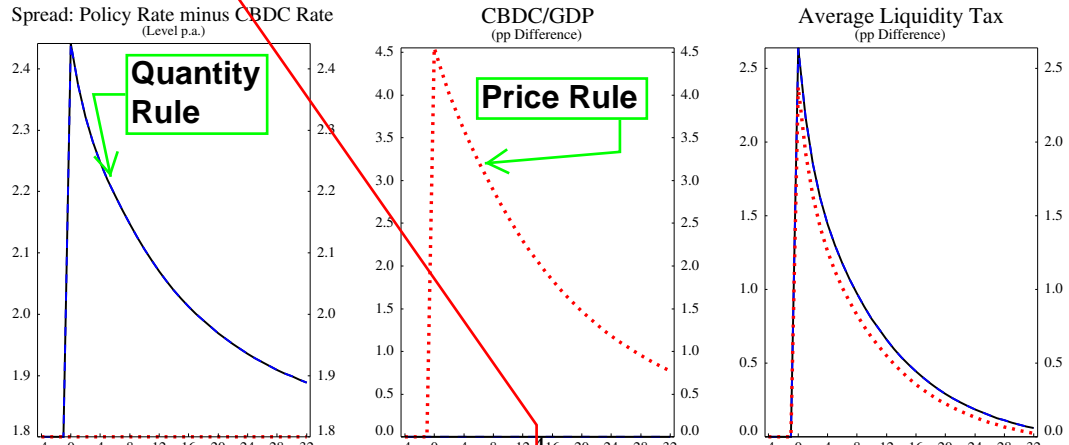
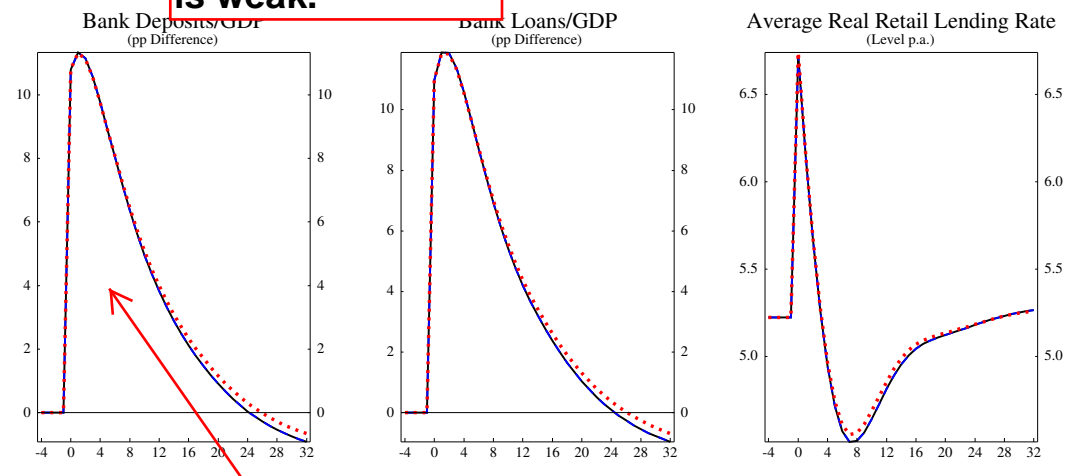
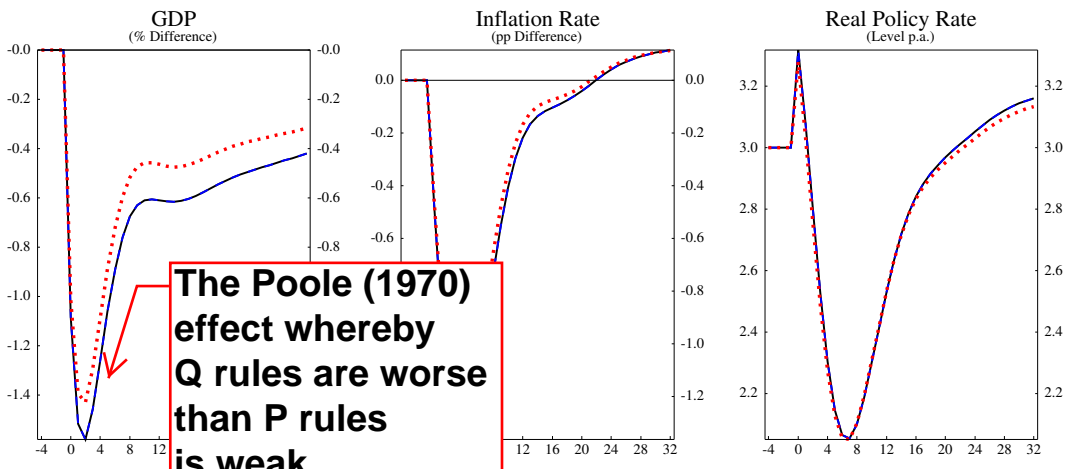
- Modern money is 95%+ created by private banks.
- This is costly: Spreads, regulation, bank market power, collateral.
- CBDC can significantly reduce these costs.
- Result: Greater money supply at reduced cost.



**Transition to Steady State with CBDC**  
solid line = actual transition ; dotted line = change in long-run steady state

## **6 Quantity Rules or Price Rules for CBDC**

A Poole (1970) contractionary money demand shock.



**Liquidity demand is mostly satisfied by instantaneous creation of bank deposits through loans. But CBDC can help.**

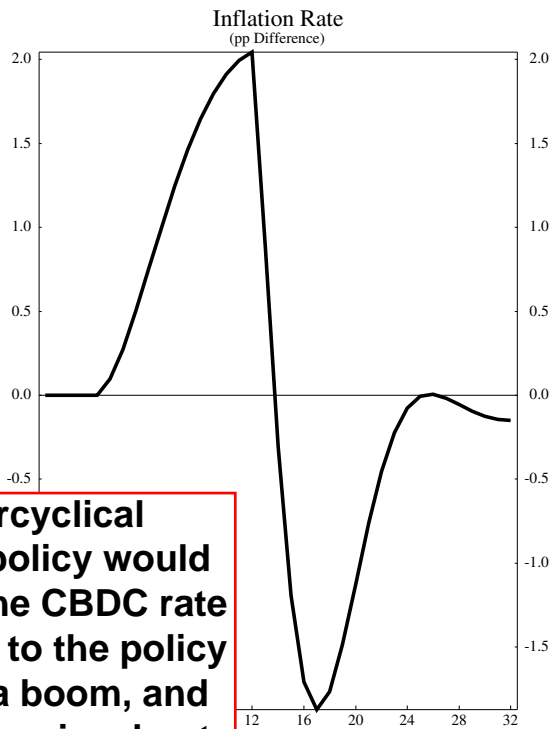
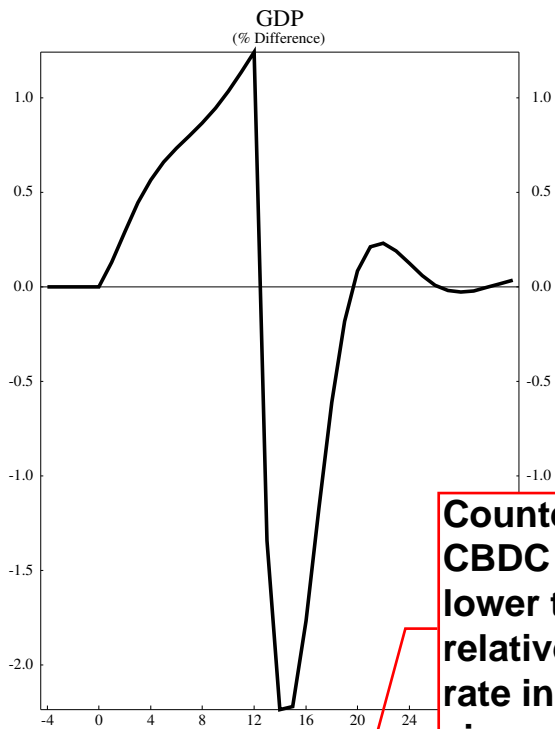
**Shock to Demand for Total Liquidity**

solid line = quantity rule ; dotted line = price rule

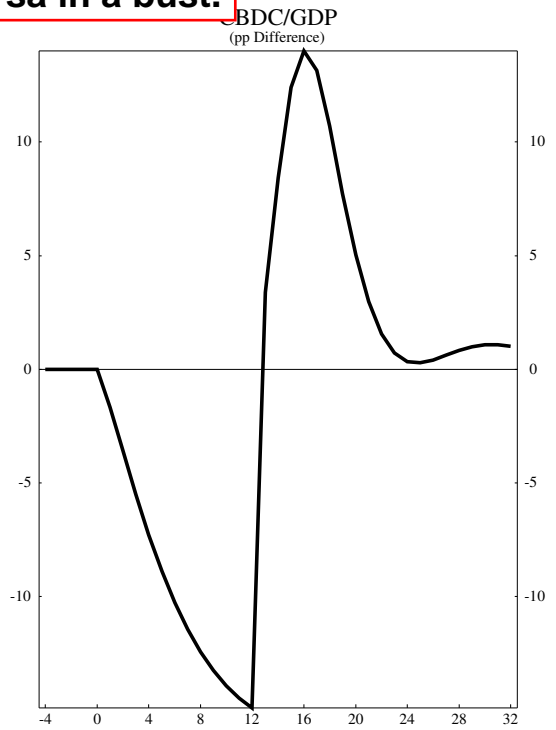
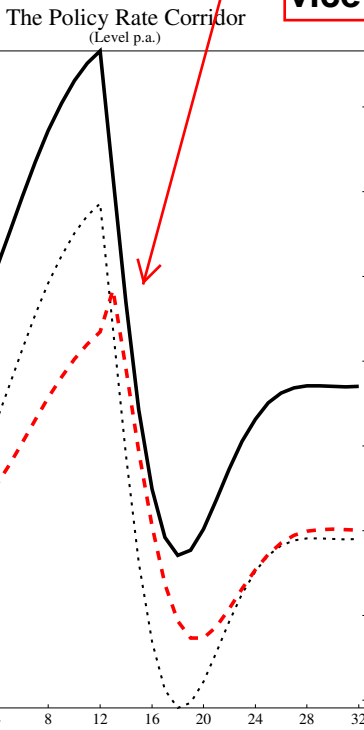
## **7 Countercyclical CBDC Rules**

A Christiano-Motto-Rostagno (2014) boom-bust credit cycle.





**Countercyclical  
CBDC policy would  
lower the CBDC rate  
relative to the policy rate in a boom,  
and vice versa in a bust.**

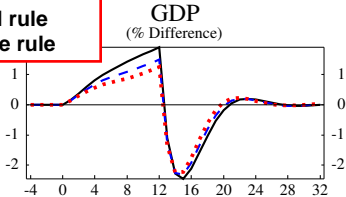


**Credit Cycle Shock - Price Rule - Policy Rate Corridor**

Bottom Left: Nominal Policy and CBDC Rates

Solid Line = Policy Rate, Dotted Line = Policy Rate minus Fixed Spread, Dashed Line = CBDC Rate

- Solid line = fixed rule
- Dashed line = cyclical rule
- Dotted line = aggressive rule



## 8 Financial Stability: CBDC Bank Runs?

- Our proposed issuance arrangements are key.
- They make deposits-to-CBDC runs very difficult in aggregate. 2 reasons:
  1. Aggregate increases in CBDC demand do not affect bank deposits:
    - Central bank sells CBDC only against government debt.
    - **Not** against bank deposits: No unconditional LoLR guarantee.
    - CBDC purchases among non-banks are irrelevant for deposits.
  2. CBDC policy rules can further discourage volatile CBDC demand.
    - Quantity rule:
      - \* CBDC supply fixed, CBDC interest rate clears the market.
      - \* **Lower political bound on CBDC rate?** Switch to price rule.
    - Price rule:
      - \* CBDC supply endogenous, CBDC quantity clears the market.
      - \* **Running out of government bonds?** Switch to other securities.

## 9 Conclusions

1. Steady state efficiency:
  - Lower interest rates, higher seigniorage, more and cheaper liquidity.
  - Increase in steady-state GDP could be as much as 3%.
2. Business cycle stability:
  - Second policy instrument.
  - Improved ability to stabilize inflation and the business cycle.
3. Financial stability:
  - CBDC should reduce many financial stability risks.
  - But if it is not designed well it may introduce others.
  - The “run risk” can be mostly eliminated by sound system design.
- Critical issue: Design of a smooth transition.

THANK YOU