

Inaccurate Statistical Discrimination: An Identification Problem

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Existence of Discrimination

Systemic **discrimination** has been well documented.

- ▶ Racial, ethnic, gender, sexual orientation.
- ▶ Documented in a variety of important markets: housing, credit, labor, online consumer markets.
- ▶ See Bertrand Duflo (2016) and Fang Moro (2011) for overview.

Literature defines two potential **sources** of discrimination

- ▶ **Taste- or preference-based discrimination:** due to **animus** against members of a group (Becker 1957).
- ▶ **Statistical discrimination:** **uncertainty** about productivity
 - ▶ Believe groups avg productivity is lower (Phelps 1972; Arrow 1973).
 - ▶ Believe group has higher variance (Aigner & Cain 1977).
- ▶ **Distinguishing** between these two types of discrimination is important for policy and welfare.
 - ▶ Methods: outcome-based tests, varying information set.
 - ▶ **Key identifying assumption:** beliefs are **accurate**.

Inaccurate Beliefs

- ▶ Evidence from psychology and economics that people have **systematic biases** in beliefs.
 - ▶ Inaccurate stereotypes based on representativeness heuristic (Bordalo et al. (2016)).
 - ▶ Enormous literature in psychology discussing how stereotypes can be inaccurate (see Fiske (2018) for review).
- ▶ Inaccurate beliefs may arise from a **lack of information**.
 - ▶ Inexperience (e.g. aliens arrive from Mars).
 - ▶ Accurate priors about population averages, but unsure how selection impacts population being evaluated (e.g. hiring & promotion criteria).
 - ▶ Knowledge of other peoples beliefs (e.g. interpreting a recommendation letter).

Why do Inaccurate Beliefs Matter?

- ▶ Evaluators use beliefs to **learn** about trait of candidate (e.g. productivity).
 - ▶ Belief about population distribution of trait.
 - ▶ Belief about how statistics (GPA, test scores) convey information about candidates trait.
 - ▶ Belief about prior evaluators beliefs (e.g. how to interpret reference).
- ▶ Inaccurate beliefs lead to **inaccurate inference** about the candidate.
 - ▶ May **persist** even in the face of a lot of information about candidate (learning literature on model misspecification).
 - ▶ May cause inefficient **exit** from market.
 - ▶ Bohren Imas Rosenberg (2019): dynamics of discrimination with inaccurate beliefs.

Important to distinguish between discrimination due to accurate vs. inaccurate beliefs

Methodological

- ▶ Relaxing assumption of accurate beliefs generates an **identification** problem.

Policy

- ▶ **Effective interventions** when beliefs are inaccurate very different than those for accurate statistical or taste-based sources.
- ▶ **Welfare implications** for inaccurate statistical discrimination differ from accurate statistical and taste-based discrimination.

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Discuss accurate versus inaccurate beliefs	11	10.5%
Test for inaccurate beliefs	7	6.7%
Measure beliefs	7	6.7%

Scope: papers published between 1990-2018 in AEJ: Applied, AEJ: Policy, AER, EMA, JEEA, JLE, JPE, ReStud, ReStat, QJE.

An Identification Problem

Worker:

- ▶ Group identity $g \in \{M, F\}$.
- ▶ Productivity $a \sim N(\mu_g, 1/\tau_g)$.
- ▶ Signal $s = a + \epsilon$, $\epsilon \sim N(0, 1/\eta_g)$.
- ▶ Focus on discrimination against group F .

Evaluator:

- ▶ Decides whether to hire worker, $v \in \{0, 1\}$.
- ▶ Holds subjective beliefs $(\hat{\mu}_g, \hat{\tau}_g, \hat{\eta}_g)$.
 - ▶ Misspecified model when subjective parameters \neq true parameters.
- ▶ Observes g and s ; uses Bayes rule to update belief about a .
- ▶ Hires worker if subjective posterior $\hat{E}_\theta[a|s, g]$ above group-specific hiring threshold $u_g \in \mathbb{R}$.
- ▶ $\theta = \{u_g, \hat{\mu}_g, \hat{\tau}_g, \hat{\eta}_g\}_{g \in \{M, F\}}$ denotes evaluator's type.

Partiality

Categorize different forms of **preferences** and **beliefs**.

- ▶ Use **partiality** to refer to properties of model primitives.
- ▶ To distinguish from **discrimination** – property of behavior and consequence of primitives.

Definition (Preference Partiality)

An evaluator has *preference partiality* if $u_F \neq u_M$.

Definition (Belief Partiality)

An evaluator has *belief partiality* if $(\hat{\mu}_F, \hat{\tau}_F, \hat{\eta}_F) \neq (\hat{\mu}_M, \hat{\tau}_M, \hat{\eta}_M)$.

Accurate if $(\hat{\mu}_g, \hat{\tau}_g, \hat{\eta}_g) = (\mu_g, \tau_g, \eta_g)$ for $g \in \{M, F\}$ and otherwise *inaccurate*.

Discrimination

Let $v(s, g, \theta) \equiv \mathbb{1}\{\hat{E}_\theta[a|s, g] \geq u_g\}$ denote optimal hiring decision.

- ▶ Difference between hiring decisions

$$D(s, \theta) \equiv v(s, M, \theta) - v(s, F, \theta).$$

- ▶ **Discrimination** occurs against group F if $\exists s$ s.t. $D(s, \theta) > 0$.
- ▶ Interested in when different sets of beliefs and preferences give rise to **same** discriminatory behavior.

Definition (Equivalent Discrimination)

Two evaluators of types θ and θ' exhibit **equivalent discrimination** if $D(s, \theta) = D(s, \theta')$ for all $s \in \mathbb{R}$.

Equivalent Discrimination

Posterior mean ability monotonic wrt s

- ▶ Represent optimal hiring decision as cut-off rule wrt signal: hire if $s \geq \bar{s}(\theta, g)$.
- ▶ Two types have same signal cut-offs \Rightarrow equivalent discrimination.

Proposition

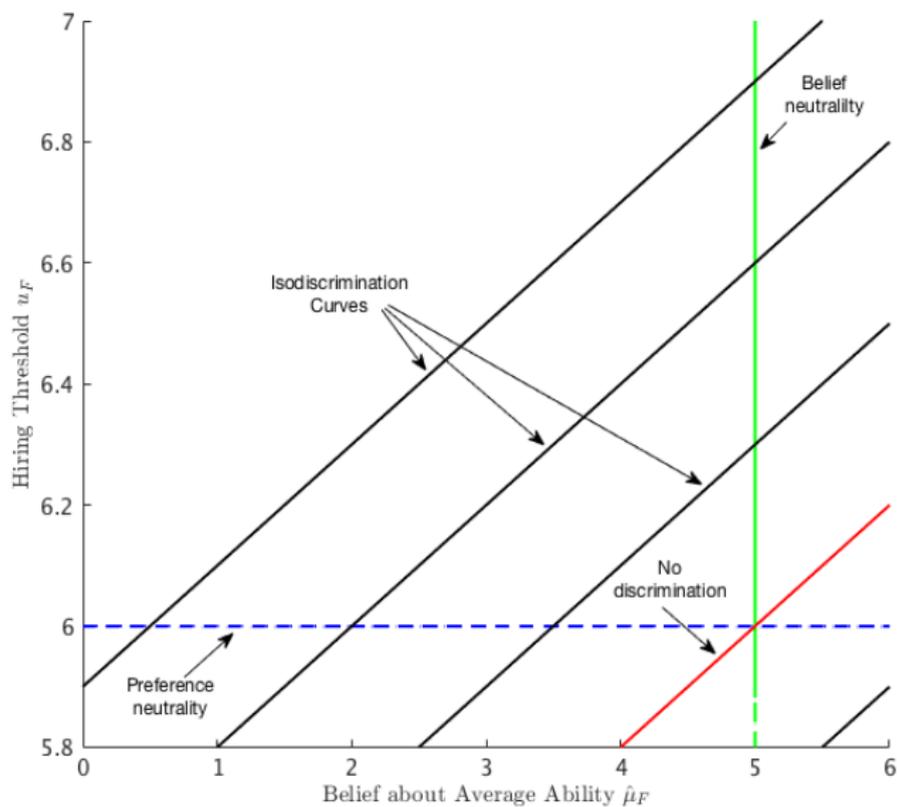
For any constants $(s_M, s_F) \in \mathbb{R}^2$ with $s_M \neq s_F$, equivalent discrimination occurs for the set of types $\{(u_g, \hat{\mu}_g, \hat{\tau}_g, \hat{\eta}_g)\}_{g \in \{M, F\}}$ s.t.

$$\frac{\hat{\tau}_M + \hat{\eta}_M}{\hat{\eta}_M} u_M - \frac{\hat{\tau}_M}{\hat{\eta}_M} \hat{\mu}_M = s_M \quad (1)$$

$$\frac{\hat{\tau}_F + \hat{\eta}_F}{\hat{\eta}_F} u_F - \frac{\hat{\tau}_F}{\hat{\eta}_F} \hat{\mu}_F = s_F \quad (2)$$

No discrimination occurs for set of types that satisfy (1) and (2) for all $s_M = s_F$.

Isodiscrimination Curves



Identifying Discrimination

Can property of interest can be backed out from available data?

- ▶ Assume, at the minimum, researcher observes group g and hiring decision v for each worker.

Existence of Discrimination

Show there exists an s such that $D(s, \theta) > 0$.

- ▶ If researcher also observes s , this is straightforward.
- ▶ Otherwise, can use **correspondence** or **audit** study: create fictitious workers with randomly assigned g and s .

Observations:

- ▶ Observing g , v and s for a set of workers from each group, with at least one signal $s \in [\bar{s}(\theta, M), \bar{s}(\theta, F))$, identifies the **existence** of discrimination.
- ▶ Observing g , v and s for a continuum of group M and F workers with signals in a neighborhood of $\bar{s}(\theta, M)$ and $\bar{s}(\theta, F)$, respectively, identifies **isodiscrimination curve**.

Source of Discrimination

Identify form of partiality that generates observed discriminatory behavior.

- ▶ Correspondence studies cannot distinguish between preference partiality and accurate belief partiality.
- ▶ Same insight extends to inaccurate belief partiality.
- ▶ Moreover, not possible to even rule out any potential sources.
 - ▶ Construct evaluator types with single category of preference or belief partiality that exhibit equivalent discrimination.
 - ▶ Establishes each form of partiality in isolation can generate given pattern of discrimination.

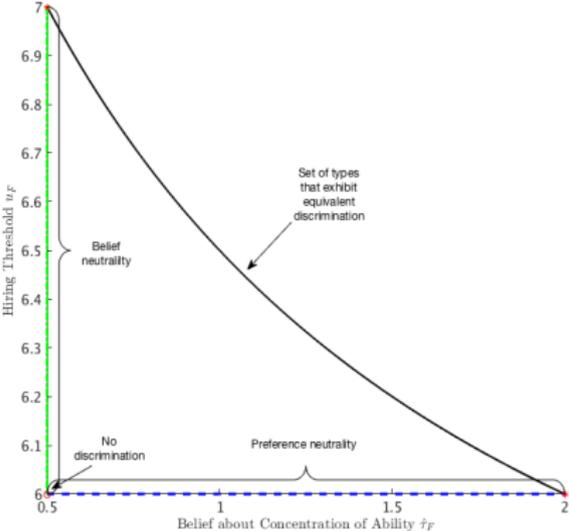
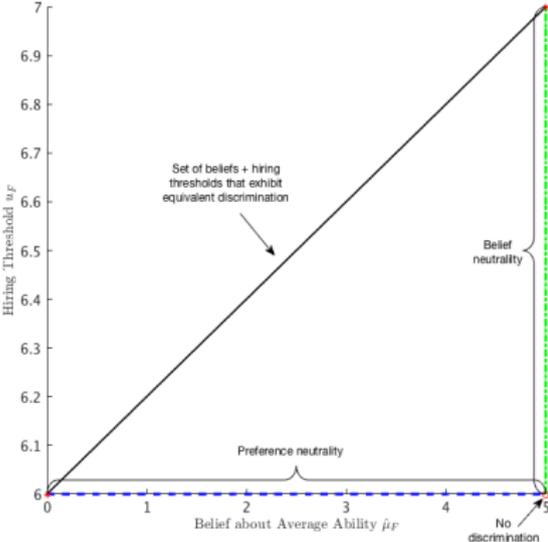
Source of Discrimination

Proposition (Equivalent Sources)

For any $(s_M, s_F) \in \mathbb{R}^2$ with $s_F > s_M$, the corresponding isodiscrimination curve includes:

1. A type with **preference partiality** and belief neutrality, $u_F > u_M$ and $(\hat{\mu}_F, \hat{\tau}_F, \hat{\eta}_F) = (\hat{\mu}_M, \hat{\tau}_M, \hat{\eta}_M)$.
2. A type with preference neutrality and belief partiality generated by **lower expected productivity**, $\hat{\mu}_F < \hat{\mu}_M$, and $(u_F, \hat{\tau}_F, \hat{\eta}_F) = (u_M, \hat{\tau}_M, \hat{\eta}_M)$.
3. A type with preference neutrality and belief partiality generated by **higher (lower) concentration of productivity**, $\hat{\tau}_F > \hat{\tau}_M$ ($\hat{\tau}_F < \hat{\tau}_M$), and $(u_F, \hat{\mu}_F, \hat{\eta}_F) = (u_M, \hat{\mu}_M, \hat{\eta}_M)$ for $\hat{\mu}_g < u_g$ ($\hat{\mu}_g > u_g$).
4. A type with preference neutrality and belief partiality generated by **lower (higher) signal precision**, $\hat{\eta}_F < \hat{\eta}_M$ ($\hat{\eta}_F > \hat{\eta}_M$), and $(u_F, \hat{\mu}_F, \hat{\tau}_F) = (u_M, \hat{\mu}_M, \hat{\tau}_M)$ for $\hat{\mu}_g < u_g$ ($\hat{\mu}_g > u_g$).

Equivalent Sources



Identifying Source

Corollary

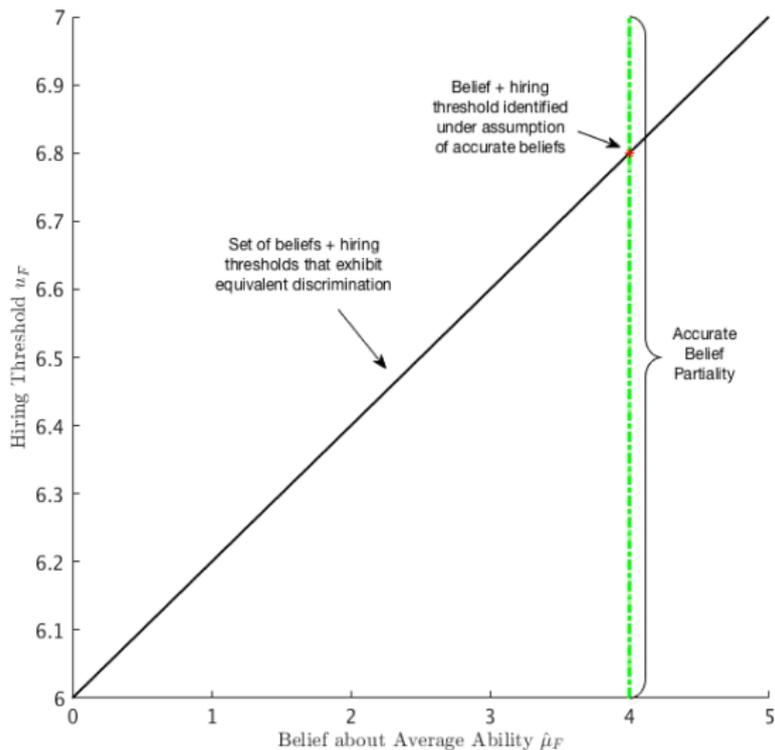
Identifying the isodiscrimination curve does not rule out any category of partiality.

Outcome-based Test.

Common method to identify source under assumption of **accurate beliefs** not valid when beliefs may be inaccurate.

- ▶ Suppose it is also possible to collect data on the productivity and signal distributions for each group.
- ▶ Under assumption of **accurate beliefs**, this identifies source.

Outcome-based Test: Accurate Beliefs



Outcome-based Test: Inaccurate Beliefs

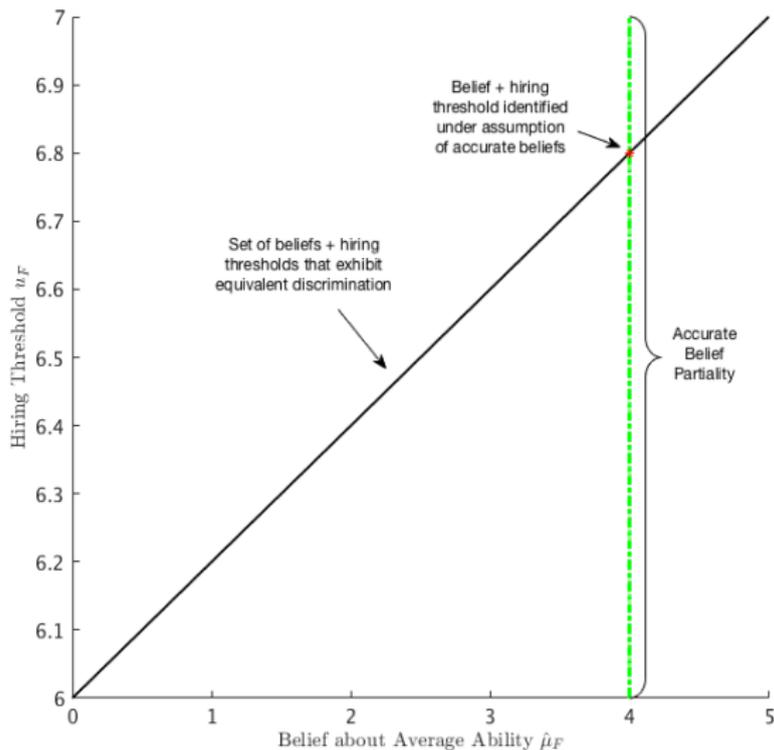
Identification crucially depends on accurate belief assumption.

- ▶ If true productivity and signal distributions identical, differential treatment may stem from preference partiality, inaccurate belief partiality, or combination of the two.
- ▶ If true productivity or signal distributions differ, differential treatment may stem from accurate beliefs (potentially coupled with preference partiality), preference partiality or inaccurate beliefs.

Observation (An Identification Failure)

Suppose a researcher observes the true productivity and signal distributions for each group and can identify the isodiscrimination curve. This does not identify the evaluator's type.

Outcome-based Test: Inaccurate Beliefs



Rejecting Accurate Statistical Discrimination

Sometimes possible to rule out accurate belief partiality as sole source of discrimination.

- ▶ See if given pattern of discrimination consistent with accurate belief partiality + preference neutrality.
- ▶ Of particular interest, since ruling out establishes discrimination stems from animus towards group or inaccurate beliefs about them.

Observation (Rejecting Accurate Statistical Discrimination)

Suppose a researcher observes the true productivity and signal distributions for each group and can identify the isodiscrimination curve with thresholds (s_M, s_F) . If

$$\frac{\tau_M \mu_M + \eta_M s_M}{\tau_M + \eta_M} \neq \frac{\tau_F \mu_F + \eta_F s_F}{\tau_F + \eta_F}, \quad (3)$$

the evaluator is not an accurate statistical discriminator.

Eliciting Beliefs.

If possible to collect data on evaluator's subjective beliefs, then can identify source.

Observation (Identifying Preferences from Beliefs)

Suppose a researcher can identify the isodiscrimination curve. Observing $(\hat{\mu}_g, \hat{\tau}_g, \hat{\eta}_g)$ identifies u_g , and therefore, the evaluator's type.

Does not identify whether beliefs are accurate – to do so, must also observe true distributions.

Experiment

Illustrative example

- ▶ Demonstrate importance of **inaccurate beliefs** in how we study discrimination.

Experiment

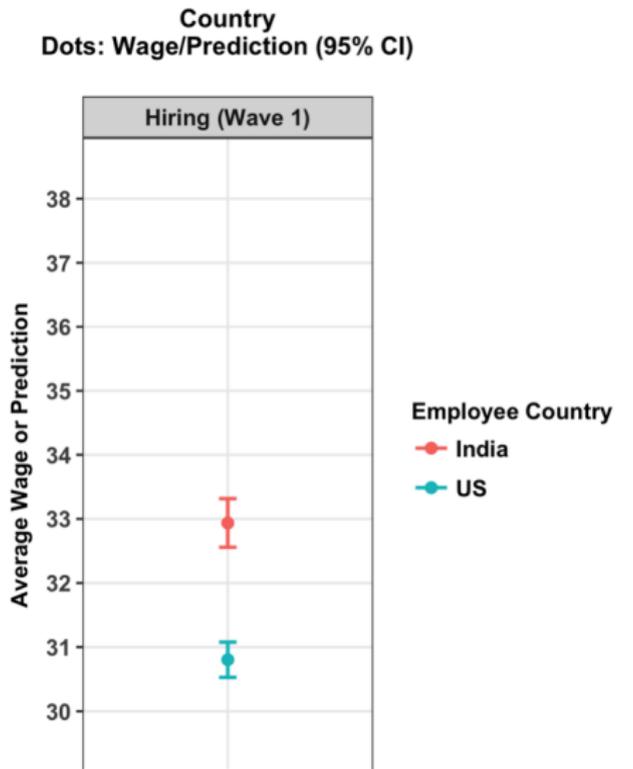
- ▶ **Part 1:** 600 Mturkers (400 from US; 200 from India) recruited to be “employees.”
 - ▶ Completed 50 question math test.
 - ▶ Answered 8 questions to develop personal profile.
- ▶ **Part 2:** 600 different Mturkers (400 from US; 200 from India) recruited to be “employers.”
 - ▶ Observed profiles of 20 different employees.
 - ▶ Decided maximum wage (wtp) to hire each (0-50 cents).
- ▶ **Payment**
 - ▶ Drawn random number x between 0 and 50 for each potential employee; if $wtp \geq x$, employer hires employee and pays wage x .
 - ▶ Employers earn 1 cent for each question that hired employee answered correctly.
 - ▶ Employers told avg # correct answers was 37.
 - ▶ Comprehension questions to check understanding.

Step 1: check for differential treatment

Three sets of **group identities** in experiment:

1. **Indian vs. American**
2. Male vs. Female
3. Old vs. Young

Indians employees receive **higher** wages than Americans



Summary

Part 1: Document Differential Treatment

- ▶ Indians favored relative to Americans.

Given the conventional pattern for studying discrimination, how would we test for statistical vs. taste-based discrimination?

Summary

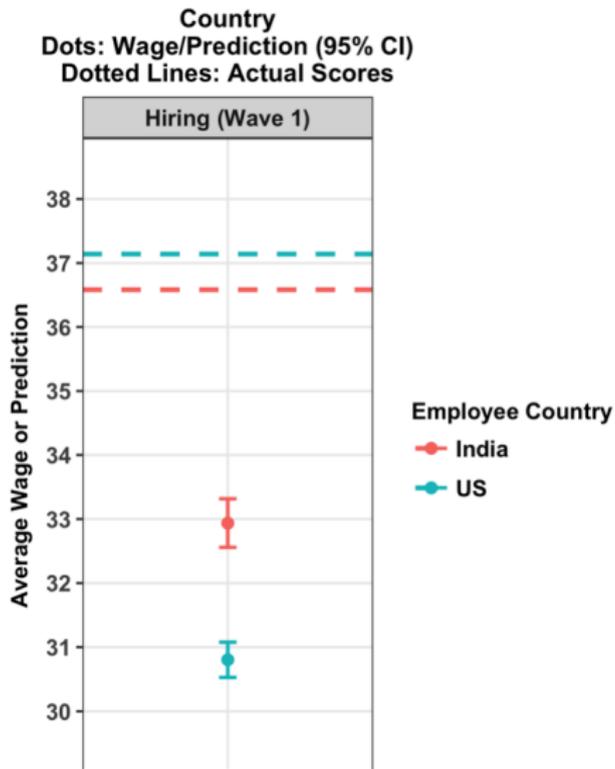
Part 1: Document Differential Treatment

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Given the conventional pattern for studying discrimination, how would we test for statistical vs. taste-based discrimination?

- ▶ Compare to **true** performance distributions.

Taste-based discrimination against Americans.



Summary

Part 1: Document Differential Treatment

- ▶ Indians favored relative to Americans.

Part 2: Compare to True Distributions (e.g. standard technique)

- ▶ Taste-based discrimination against Americans.

But what if beliefs are wrong?

Part 3: Elicit Average Beliefs

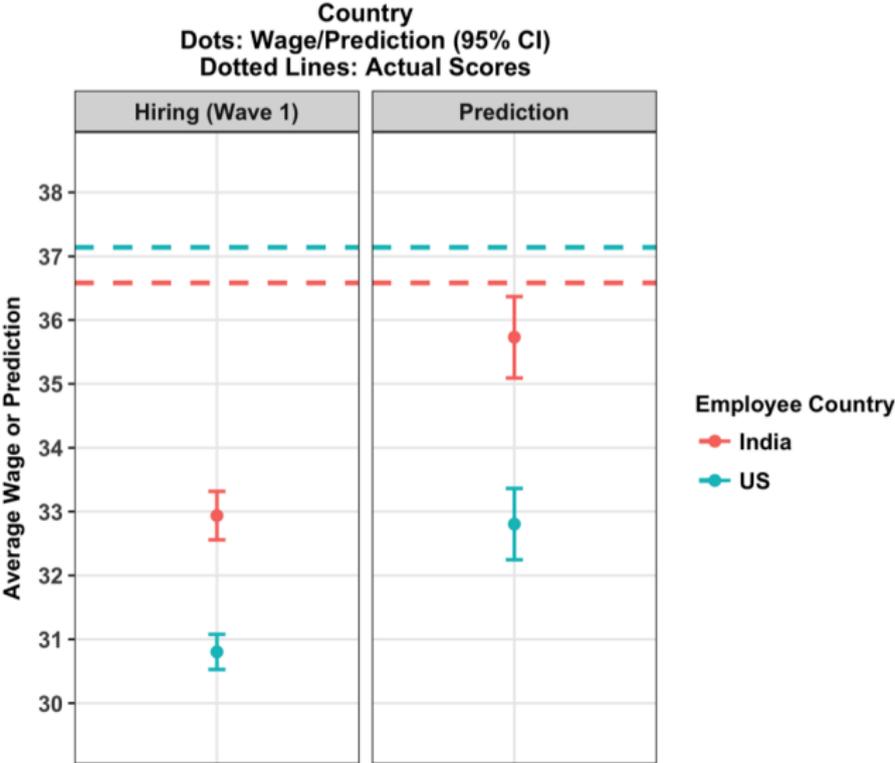
Employers asked following question:

“On average, how many questions do you think g answered correctly?”

where $g \in \{Americans, Indians\}$.

- ▶ Provided incentive compatible bonuses for performance on questions.
- ▶ Randomized between small and large incentives – no differences between two groups.

Inaccurate statistical discrimination against Americans.



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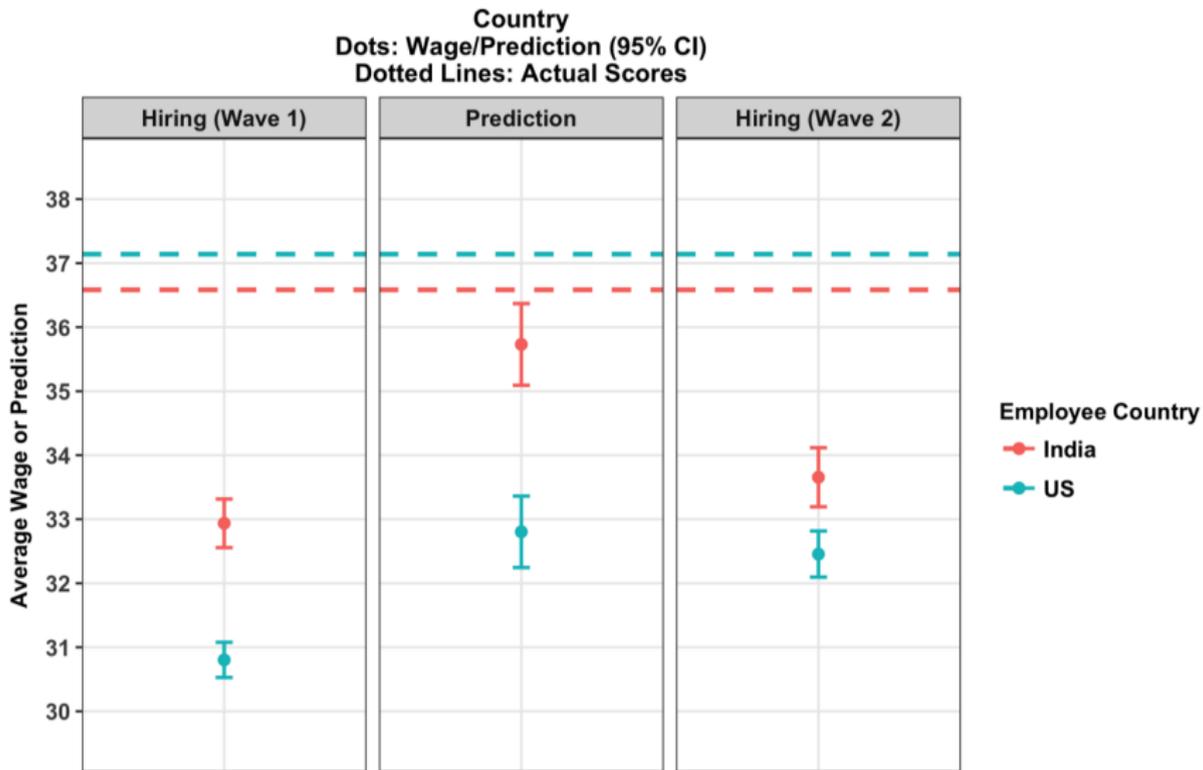
Part 3: Compare True and Perceived Distributions

- ▶ Inaccurate statistical discrimination against Americans.

Intervention: is it possible to correct beliefs?

- ▶ Employers were told *“Here are the correct answers for the belief questions that you answered.”*
 - ▶ Americans answered 37.14 questions correctly on average.
 - ▶ Indians answered 36.58 questions correctly on average.
- ▶ Asked to make wage offers based on 10 additional employee profiles (same hiring/payment scheme).

Either **taste-based** or still some **inaccurate** statistical discrimination against Americans.



P-Value for Wave 2 - Wave 1 Difference: 0.014

Conclusions

Inaccurate beliefs may be prevalent in many domains currently being studied by discrimination researchers.

- ▶ Most tests to separate statistical and taste-based sources rely on strong assumption: people hold **accurate** beliefs.
- ▶ Incorrectly imposing this assumption can lead to **mistaken attribution** of source, and therefore, misguided policy/welfare analysis.
- ▶ Relaxing this assumption generates an **identification** problem.
- ▶ Illustrative example using results from an online experiment demonstrates the **importance of inaccurate beliefs** in how we study discrimination.

Conclusions: Two Key Forms of Inaccurate Beliefs

Inaccurate **priors** / beliefs about population.

- ▶ Persistent discrimination due to selection effects / exit
- ▶ May not “wash out” in the long-run.
- ▶ Discrimination reversals can be sign of selection (Bohren Imas Rosenberg (2019)).

Inaccurate **beliefs about signals**.

- ▶ Persistent discrimination due to incorrect updating.
- ▶ Could be about exogenous signals (e.g. how predictive is a test) or endogenous signals (e.g. interpreting reference letter).